

不定積分と定積分の計算練習 60 題

- $$1. \int \sqrt[5]{x^4} dx = \frac{5}{9} x^{\frac{9}{5}} + C$$
- $$2. \int \frac{3 + \cos^3 x}{\cos^2 x} dx = 3 \tan x + \sin x + C$$
- $$3. \int e^{3x+1} dx = \frac{1}{3} e^{3x+1} + C$$
- $$4. \int \cos 2x dx = \frac{\sin x}{2} + C$$
- $$5. \int \cos^2 x dx = \frac{x}{2} + \frac{\sin 2x}{4} + C$$
- $$6. \int \frac{3}{x} dx = 3 \log |x| + C$$
- $$7. \int \frac{e^x - e^{-x}}{e^x + e^{-x}} dx = \log(e^x + e^{-x}) + C$$
- $$8. \int_{-\pi}^{\pi} \sin x \cos^2 x dx = 0$$
- $$9. \int_{-\pi}^{\pi} \sin^3 x dx = 0$$
- $$10. \int_{-1}^1 x e^{x^2} dx = 0$$
- $$11. \int_{-1}^1 \sin x e^{\cos x} dx = 0$$
- $$12. \int_{-\pi}^{\pi} \frac{\sin x}{\cos x + 2} dx = 0$$
- $$13. \int \sin(3x - 2) dx = -\frac{1}{3} \cos(3x - 2) + C$$
- $$14. \int (2x + 1) \sqrt{x + 2} dx = \frac{5}{4} (x + 2)^{\frac{3}{2}} (x - \frac{1}{2}) + C$$
- $$15. \int \frac{x}{1 + x^2} \log(1 + x^2) dx = \frac{1}{4} (\log(1 + x^2))^2 + C$$

16. $\int x e^{3x} dx = \frac{1}{3} x e^{3x} - \frac{1}{9} e^{3x} + C$
17. $\int \sqrt{x} \log x dx = \frac{2}{3} x^{\frac{3}{2}} \log x - \frac{4}{9} x^{\frac{3}{2}} + C$
18. $\int x \sin(2x + 1) dx = -\frac{x}{2} \cos(2x + 1) + \frac{\sin(2x + 1)}{4} + C$
19. $\int \frac{x^2 + 1}{x + 1} dx = \frac{x^2}{2} - x + 2 \log |x + 1| + C$
20. $\int \frac{x + 5}{(x + 1)(x - 3)} dx = \log \left| \frac{|x - 3|^2}{x + 1} \right| + C$
21. $\int \sin x \cos 3x dx = -\frac{\cos 4x}{8} + \frac{\cos 2x}{4} + C$
22. $\int \frac{\sin x \cos x}{1 + \sin x} dx = -\log |1 + \sin x| + \sin x + C$
23. $\int \frac{1}{\sqrt{2x + 3} - \sqrt{2x}} dx = \frac{1}{9} (2x + 3)^{\frac{3}{2}} + \frac{(2x)^{\frac{3}{2}}}{9} + C$
24. $\int \frac{1}{\cos x} dx = \frac{1}{2} \log \left| \frac{1 + \sin x}{1 - \sin x} \right| + C$
25. $\int \frac{\log x}{x(\log x + 1)^2} dx = \log |\log x + 1| + \frac{1}{\log x + 1} + C$
26. $\int \frac{e^{2x}}{e^x - 1} dx = e^x + \log |e^x - 1| + C$
27. $\int \frac{5^{2x}}{2 \log 5} dx = \frac{5^{2x}}{(2 \log 5)^2} + C$
28. $\int \frac{3(x^2 - 4x)}{x^3 - 6x^2 + 3} dx = \log |x^3 - 6x^2 + 3| + C$
29. $\int x e^{-\frac{1}{3}x} dx = -3x e^{-\frac{x}{3}} - 9e^{-\frac{x}{3}} + C$
30. $\int \frac{x + 4}{x(x + 2)} dx = \log \left| \frac{x^2}{x + 2} \right| + C$

31. $\int 2 \sin^2 x dx = x - \frac{\sin 2x}{2} + C$
32. $\int_1^3 x^{-3} dx = \frac{4}{9}$
33. $\int_0^1 \sqrt{e^{1-x}} dx = 2(e^{\frac{1}{2}} - 1)$
34. $\int_1^e \frac{\log x}{x} dx = \frac{1}{2}$
35. $\int_0^1 x^2 e^{x^3} dx = \frac{1}{3}(e - 1)$
36. $\int_0^2 x e^x dx = e^2 + 1$
37. $\int_e^{e^2} \log x dx = e^2$
38. $\int_{e^2}^{e^3} \frac{1}{x} dx = 1$
39. $\int_0^\pi \sin x dx = 2$
40. $\int_0^{\frac{\pi}{6}} \frac{1}{\cos^2 x} dx = \frac{1}{\sqrt{3}}$
41. $\int_0^{\frac{\pi}{2}} \frac{\sin x}{2 + \cos x} dx = \log \frac{3}{2}$
42. $\int_{-2}^2 \frac{1}{x^2 + 4} dx = \frac{\pi}{4}$
43. $\int_0^2 \frac{1}{\sqrt{16 - x^2}} dx = \frac{\pi}{6}$
44. $\int_0^1 \frac{e^x - 1}{e^x + 1} dx = \log \frac{(e + 1)^2}{4e}$
45. $\int_1^2 e^{\sqrt{x}} dx = 2(\sqrt{2} - 1)e^{\sqrt{2}}$

$$46. \int_0^2 x^3 \sqrt{4-x^2} dx = \frac{64}{15}$$

$$47. \int_0^{\frac{\pi}{2}} \frac{\sin^3 x}{1+\cos x} dx = \frac{1}{2}$$

$$48. \int_0^1 \frac{3e^x}{e^x+1} dx = 3 \log \frac{e+1}{2}$$

$$49. \int_0^1 \sqrt{4-x^2} dx = \frac{\pi}{3} + \frac{\sqrt{3}}{2}$$

$$50. \int_1^{\sqrt{3}} \frac{1}{x^2+3} dx = \frac{\pi}{12\sqrt{3}}$$

$$51. \int_0^1 \frac{x^2}{\sqrt{2-x^2}} dx = \frac{\pi}{4} - \frac{1}{2}$$

$$52. \int_1^e x \log x dx = \frac{e^2}{4} + \frac{1}{4}$$

$$53. \int_0^1 x^2 e^{2x} dx = \frac{1}{4}(e^2 - 1)$$

$$54. \int_1^e (\log x)^2 dx = e - 2$$

$$55. \int_0^{\frac{\pi}{2}} e^x \sin x dx = \frac{e^{\frac{\pi}{2}} + 1}{2}$$

$$56. \int_0^{\pi} e^x \cos x dx = -\frac{e^{\pi} + 1}{2}$$

$$57. \int_1^4 \frac{1}{x^2 - 2x + 4} dx = \frac{\pi}{3\sqrt{3}}$$

$$58. \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \tan^2 x dx = \frac{2}{\sqrt{3}} - \frac{\pi}{6}$$

$$59. \int_{\log \frac{1}{\sqrt{3}}}^{\log \sqrt{3}} \frac{e^x}{e^{2x} + 1} dx = \frac{\pi}{6}$$

$$60. \int_0^{\frac{\pi}{2}} \frac{\sin x}{\sin x + \cos x} dx = \frac{\pi}{4}$$