## Simplex Algorithm

## November 7, 2016

## Abstract

This is pseudocode for the core of the Simplex Algorithm, adapted from *A Gentle Introduction to Optimization*.

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Algorithm 2.1 Simplex Algorithm
   Input: Linear program (P) and feasible basis B
   Output: An optimal solution for (P) or a certificate proving that (P) is
1 Rewrite (P) so that it is in canonical form for the basis B
2 Let \vec{x} be the basic feasible solution for B
\vec{a} if \vec{c_N} \leq \vec{0} then
        stop
        (\vec{x} \text{ is optimal})
8 Select k \in N such that c_k > 0
9 if A_k \leq \vec{0} then
10 {
11
        stop
        ((P) is unbounded)
13 }
14 Let r be any index i where the following minimum is attained:
                                  t = \min\left\{\frac{b_i}{A_{i,k}} : A_{i,k} > 0\right\}
                                                                                                (1)
16 Let \iota be the r^{th} basis element
17 Set B := B \cup \{k\} \setminus \{\iota\}
```

## Notes:

18 Go to step 1

1. Recall  $\vec{c}$  is the vector of coefficients in our objective function  $z(\vec{x})$ , and  $c_k$  is the kth element of  $\vec{c}$ .

- 2.  $\vec{c_N}$  is  $\vec{c}$  with the columns corresponding to basis B removed.
- 3. A is the  $m \times n$  matrix with linearly independent rows that comprise our constraints.  $A_k$  is the kth column of A (a vector, though we aren't writing it with the arrow above), and  $A_B$  or  $A_N$  is a matrix comprised of a subset of the columns of A, keeping them in the original order.